

Federal Reserve Bank of Minneapolis
Research Department

March 2020

Quantifying Efficient Tax Reform*

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ABSTRACT

This paper quantifies welfare gains from Pareto reforms in an overlapping generations framework with policies constrained due to private information about shocks to household labor productivity. We use administrative panel data for the Netherlands to first estimate key parameters under status quo policies for households in different education groups. We then solve for Pareto optimal reforms and decompose the source of welfare changes into gains from level effects and gains from improved insurance. For our baseline parameterization, we find large welfare gains, on the order of 17 percent of lifetime consumption. Optimal consumption allocations are higher and more smooth than allocations under current policy, while leisure allocations are lower and more volatile. We show that the welfare decomposition is quantitatively sensitive to estimates of wage profiles and processes governing shocks to labor productivity.

Keywords: income tax reform

JEL classification: E13, H21

*Boerma acknowledges support from the Heller-Hurwicz Economic Institute, and McGrattan acknowledges support from the NSF. The views expressed herein are those of the authors and not necessarily those of the Federal Reserve Bank of Minneapolis or the Federal Reserve System.

1. Introduction

This paper quantifies welfare gains from Pareto reforms in an overlapping generations framework with policies constrained due to private information about shocks to household labor productivity. We use administrative panel data for the Netherlands to first estimate key parameters under status quo policies for households in different education groups. We then solve for Pareto optimal reforms and decompose the source of welfare changes into gains from level effects and gains from improved insurance.

To model the Netherlands, we use a small open economy framework with overlapping generations and households that are heterogeneous in age, education, and productivity. Fiscal policy in this economy is summarized by tax schedules on incomes and assets and a tax rate on consumption. We compute values under current policy and use them—along with estimates for preferences, technologies, and wage processes—as inputs to our reform problem. In the reform problem, we compute the maximum consumption equivalent gain, which is restricted to be the same for all households.

For our baseline parameterization, we find large welfare gains, on the order of 17 percent of lifetime consumption. Optimal consumption allocations are higher and more smooth than allocations under current policy, while leisure allocations are lower and more volatile. To investigate this further, we decompose the total gain into contributions for level effects and contributions for improved insurance—for consumption and leisure. Increasing mean consumption is by far the largest source of gain, although some education groups with high variability in wages also have significant gains in lowering consumption dispersion.

We also show that the welfare decomposition is quantitatively sensitive to estimates of wage profiles and processes governing shocks to labor productivity. We explore two

variations of the baseline model. First, we turn off growth in wages over the life cycle. In this case, the gains from smoothing consumption are close to zero, even for households with significant variation in their labor productivity shocks. Second, we lower the variances of shocks for all households. Here again, we find a significant effect on estimates of the gains for lowering dispersion in allocations.

This paper is related to the literature on optimal income taxation. We extend Kapicka (2013), Farhi and Werning (2013), and Golosov, Troshkin, Tsyvinski (2016) to compute Pareto reforms using a baseline matched to the Netherlands with a more general productivity process. Like Hosseini and Shourideh (2019), we compute the set of Pareto improving policy reforms, but we allow for stochastic productivity shocks. We find that allowing for stochastic shocks is quantitatively important for our welfare decomposition.

2. Theory

In this section, we describe the positive economy that is our baseline for estimating key parameters of preferences, technologies, and current fiscal policies of an actual economy. We then describe the associated planning problem used to quantify Pareto reforms of the original OLG economy.

2.1. Positive Economy

In this section, we describe the model economy that will be matched up to administrative data for the Netherlands. The environment is relatively standard with the exception of country-specific fiscal policies. There are a large number of households facing uninsurable productivity risks and perfectly competitive firms with constant-returns-to-scale technologies.

Households differ by age j , assets a , and productivity ϵ . They solve the following dynamic program:

$$v_j(a, \epsilon; \Omega) = \max_{c, n, a'} \{U(c, \ell) + \beta E[v_{j+1}(a', \epsilon'; \Omega) | \epsilon]\}$$

subject to the budget constraint

$$a' = (1 + r)a - T^a(ra) + w\epsilon n - T^n(j, w\epsilon n) - (1 + \tau_c)c$$

and a lower bound on asset holdings: $a' \geq 0$. The aggregate state vector contains prices and policies:

$$\Omega = \{r, w, G, B, T^a, T^n, \tau_c\},$$

where r is the interest rate, w is the wage rate, G is government consumption, B is external debt, $T^a(\cdot)$ is the tax schedule for financial assets, $T^n(\cdot)$ is the tax schedule for labor income less transfers, and τ_c is the tax rate on consumption.

We assume the economy is small and open with interest rates r set in international markets. Firm technologies are constant-returns-to-scale functions in capital K and labor N with output Y given by:

$$Y = F(K, N).$$

Thus, knowing r , we also know the aggregate capital-labor ratio K/N and the wage rate w from the firm's optimality conditions. For computations below, we assume that prices and policies are fixed.¹ In a competitive equilibrium, the resource constraint must also hold in all periods:

$$C_t + K_{t+1} - (1 - \delta)K_t + G_t + B_{t+1} - RB_t = Y_t.$$

¹ This assumption that policies are fixed can easily be relaxed without adding much computational burden as shown by Nishiyama and Smetters (2014).

The key outputs obtained from computing equilibria for the positive economy are the values under current policy, namely

$$\vartheta(\epsilon^{j-1}) = E[v_j(a, \epsilon; \Omega) | \epsilon^{j-1}]$$

or, in the case of future generations $\vartheta(\epsilon_0) = E[v_1(a, \epsilon; \Omega) | \epsilon_0]$. We want to Pareto improve on these value, ideally by shifting the allocations to the efficient frontier. As an example, consider the two-person case drawn in Figure 1. The allocation for the Netherlands (point NL) is the result of calculating the equations above. In the next section, we compute a reform problem that puts households on the efficient frontier, at a point with their consumption levels higher by the same percentage (say, Δ).

2.2. Reform Problem

In this section, we describe the planning problem that we solve to compute Pareto reforms given the initial valuations from the positive economy.

As in the positive economy, the interest rate r is given as we are working with a small open economy. Given the production function $F(K, N)$, we can determine the optimal capital-labor ratio K/N and, hence, the marginal product of labor w . We also assume that the planner must finance government spending $\{G_t\}$ and takes the initial assets $B_0 + K_0$ as given.

Given the initial values for all households, the planning problem is to choose a feasible allocation that maximizes excess initial resources so that remaining lifetime values exceed their initial values for all households. Formally, the planning problem is:

$$\max F(K_0, N_0) + RB_0 - C_0 - K_1 + (1 - \delta)K_0 - G_0 - B_1$$

subject to the laws of motion for capital and the resource constraints for all periods, along

with incentive constraints that ensure truthful reporting of households private productivity, and a condition such that lifetime value exceeds the given initial value. In the appendix, we prove that an allocation is Pareto efficient if and only if it solves the planning problem, taking as given initial values that are generated by this allocation.

It turns out that the Lagrange function for the planning problem is separable in the allocation of each household and, therefore, we can separately characterize the solution to the planning problem for each household. The planner problem for each household is to choose a household allocation to maximize excess resources subject to the household's incentive constraints. To make this tractable, we assume that only local downward incentive constraints bind at the solution. Assuming that only the local downward incentive constraints bind is a finite type analog for the first-order approach typically adopted in dynamic Mirrlees problems with a continuum of productivity types. (See, for example, Kapicka (2013), Farhi and Werning (2013), and Golosov, Troshkin, and Tsyvinski (2016).) The relaxed component planner problem is formulated by replacing the set of constraints that ensure global incentive compatibility in the component planning problem with the set of constraints that ensure the allocation satisfies all local downward incentive constraints. We write the relaxed component planner problem recursively and then characterize its solution.

This relaxed recursive problem can be formalized as follows. The planner chooses sequences of consumption $c_j(\epsilon)$, labor $n_j(\epsilon)$, promised values $V_j(\epsilon)$ for telling the truth about the productivity type, and threat values $\tilde{V}_j(\epsilon)$ for reporting a productivity type of ϵ while being one level more skilled, which we denote by ϵ^+ . The recursive planning problem

is given by:

$$\Pi_j(V_-, \tilde{V}_-, \epsilon_-) \equiv \max \sum_{\epsilon_i \in \mathcal{E}} \pi_j(\epsilon_i | \epsilon_-) \left(w_t \epsilon_i n_j(\epsilon_i) - c_j(\epsilon_i) + \Pi_{j+1}(V_j(\epsilon_i), \tilde{V}_j(\epsilon_{i+1}), \epsilon_i) / R \right)$$

subject to:

$$\begin{aligned} U(c_j(\epsilon_i), \ell_j(\epsilon_i)) + \beta V_j(\epsilon_i) \\ \geq U(c_j(\epsilon_{i-1}), \ell_j^+(\epsilon_{i-1})) + \beta \tilde{V}_j(\epsilon_i), \text{ for } i = 2, \dots, N \end{aligned} \quad (2.1)$$

$$V_- = \sum_{\epsilon_i \in \mathcal{E}} \pi_j(\epsilon_i | \epsilon_-) \left(U(c_j(\epsilon_i), \ell_j(\epsilon_i)) + \beta V_j(\epsilon_i) \right) \quad (2.2)$$

$$\tilde{V}_- = \sum_{\epsilon_i \in \mathcal{E}} \pi_j(\epsilon_i | \epsilon_-^+) \left(U(c_j(\epsilon_i), \ell_j(\epsilon_i)) + \beta V_j(\epsilon_i) \right), \quad (2.3)$$

where $\pi_j(\epsilon_i | \epsilon_-^+)$ is the conditional probability over current states ϵ_i for households that were one level more productive in the previous period ϵ_-^+ . The first set of constraints in (2.1) ensures that utility is higher under truth-telling, with the leisure arguments given by:

$$\ell_j(\epsilon_i) = 1 - n_j(\epsilon_i)$$

$$\ell_j^+(\epsilon_{i-1}) = 1 - n_j(\epsilon_{i-1}) \epsilon_{i-1} / \epsilon_i.$$

When calculating the welfare of efficient reform, we replace V_- in the problem above at the initial age with $\vartheta(\epsilon_0) + \vartheta_\Delta$, where $\vartheta(\epsilon_0)$ is the initial value for future generations—that is, $E[v_1(0, \epsilon; \Omega) | \epsilon_0]$ in the positive economy—and the ϑ_Δ is the value corresponding to giving Δ more consumption to households.

3. Data and Estimation

In this section, we discuss the administrative data from the Netherlands and estimation methods used to parameterize the model. We start with aggregated data from the national

accounts, flow of funds, population censuses, and tax authorities. We then discuss the micro data on earnings, hours, and education.

3.1. Aggregate Data

The main data source for the aggregate data is the Dutch Bureau of Statistics. These data are publicly available.

3.1.1. National accounts

The primary data source for national income and product accounts is the *nationale rekeningen*. Table 1 splits national income by factor of production. Labor income includes compensation of employees and 70% of proprietors' income. All other income is categorized as capital income, which we adjust in three ways. First, we subtract product-specific taxes as measured in the government's income and expenditure accounts. We make this correction because we are interested in production at producer prices rather than at consumer prices. Second, we impute capital services for consumer durables—which we treat as investment—and government capital. The imputed services are assessed to be 4 percent of the current-cost net stock of consumer durables and government fixed assets. Government fixed assets as well as consumer durables are recorded as non-financial balances. Finally, we impute depreciation of consumer durables. Since our data do not include the equivalent of the United States flow of funds, we assume the ratio of consumer durable depreciation to consumer durable goods to be identical to the United States.² This implies consumer durable depreciation of 5 percent.

On the product side, revisions must also be made with regard to sales taxes, capital

² See Table 1 in McGrattan and Prescott (2017).

services and consumer durables depreciation. The sales taxes are assumed to primarily fall on personal consumption expenditures. We assume pro rata shares when assessing how much of the taxes are on durables, non-durables and services. We include nondurables and services with consumption and durable goods with tangible investment. Therefore, we subtract sales taxes from both product categories. Imputed capital services only affect our consumption measure, which combines personal and government consumption from the national accounts. The consumption of consumer durables depreciates the outstanding stock of durables, which motivates us to classify consumer durables depreciation as consumption.

Fixed assets and other capital stocks used in our analysis are shown in Table 2 with averages for 2000-2010. As in the case of national accounts, we divide all estimates by adjusted GDP. We add the stock of consumer durables. The data are separated for businesses, households, and the government. We also include the value of land, which is much higher than estimates reported by McGrattan and Prescott (2017) for the United States. In fact, the data show that the value of residential land exceeds the value of structures by roughly 12 percent, likely due to strict land-use regulation. Since the oil and gas sector is so significant for the Netherlands, we include reserves. Related to fixed assets are the valuations in flow of funds data which we report in Table 3. Here, we report estimates for household net worth and government debt relative to GDP averaged over the sample 2000-2010.

Finally, in Table 4, we report aggregates on population and hours, which we use to parameterize preferences and to check aggregated micro data. Averaging data between 2000 and 2010, we estimate that the Dutch population worked 12,243 million hours, implying average annual hours of 1,135 for every individual between ages 16 and 64.

The data from the national accounts and population census are used to parameterize the discount factor, the capital share, the depreciation rate, the weight on leisure in preferences, the length of working life, and the length of retirement.

3.1.2. Fiscal Policy

In Figure 2, we plot the income tax schedule for the Netherlands during our sample period. The figure shows three marginal tax rates, namely, 34, 42 and 52 percent for working age households, with cutoff levels of 20,000 and 59,000 Euro. Marginal tax rates are reduced for retirees with incomes below 35,000 Euro. Specifically, the marginal tax rate is 17 percent for incomes below 20,000 Euro and 24 percent for incomes below 35,000 Euro. In Figure 3, we show the tax schedule for financial assets. Below 46,000 Euro, the tax rate is 0. Above this level, the rate of taxation is 1.2 percent. Finally, we assume an effective tax rate on consumption of 13.4 percent, which is the weighted average VAT for a basket of goods in the Netherlands. These schedules and rates are used to parameterize T^a , T^n , and τ_c .

3.2. Micro Data

We use linked administrative records between 2006 and 2014 from Statistics Netherlands for the information on education, earnings, and hours—series that we need to estimate productivity processes $\{\epsilon\}$ and wage profiles $\{\zeta\}$ over the life cycle for different education groups.

3.2.1. Merged datasets

We start with a representative subsample of all Dutch households selected by Statistics

Netherlands. The sample consists of roughly 95 thousand households per year, which is 1.3 percent of the population of households, covering a total of over 275 thousand individuals. For all analyses, we weight households with the provided sample weights. We consider all households with heads of household above age 25. Income is measured by employer-provided earnings records. We construct an individual’s annual taxable labor earnings, which includes the employer’s health insurance contribution, by adding all earnings reports within a given calendar year. To construct an hourly wage rate, we merge the earnings dataset with a dataset on employer-reported hours worked, dividing taxable labor earnings by hours of work. Because the model features a single decision maker for each household, we define the household wage rate for married and cohabitating households as the average individual wage rate weighted by the hours worked of each partner. For single households, the individual wage rate is the household wage rate. Household non-market time is given by average individual non-market time which is discretionary time minus individual hours worked. We set an individual’s discretionary time equal to 16 hours a day for 365 days.

We merge the datasets for earnings and hours with another that provides education levels for our sample. We need this information because we assume that there is ex-ante heterogeneity in productivity and wage profiles based on the highest educational degree earned. We classify every degree as a low, a medium, or a high level of education. The low education level is a high school degree or a practical degree, the medium level is a degree from a university of applied sciences, and the high level is a university degree. We group households into six education bins, which are unordered pairs of the degree of each partner. Singles are grouped with couples in which both partners have obtained the same level of education.³

³ In our sensitivity analysis, we also explore conditioning on head of household, which is more common in the literature.

We should note here that there are significant advantages to the merged data available in the Netherlands relative to what is available in most other countries. For example, in the case of the United States, we only have administrative data for earnings whereas in the Netherlands we have earnings and hours linked and available for all members of the household. We also have detailed data on education, which is not available in the United States.

3.2.2. *Estimated wage processes*

We estimate the parameters that govern the residual wage process using the minimum distance estimator (Chamberlain (1984)). We first regress logarithmic wages on as follows:

$$\log W_{ijt} = A_t + X_{ijt} + \omega_{ijt},$$

where the household index is i , age is j , and the period is t . The right-hand-side variables are time effects A_t and household observables X_{ijt} . The observables include a set of dummy variables for the age of the household head, the coefficient of which is our estimate of the lifecycle profile ζ_j .

The second step is to estimate components of the residual wage after pooling across cohorts. More specifically, we use the method of simulated moments approach to estimate parameters $\rho, \sigma_u^2, \sigma_\eta^2, \sigma_{\epsilon_0}^2$ for the standard permanent-transitory process:

$$\omega_{ij} = \epsilon_{ij} + \eta_{ij}$$

$$\epsilon_{ij} = \rho\epsilon_{ij-1} + u_{ij}$$

with the persistent component of the residual wages given by ϵ_{ij} and the transitory component given by η_{ij} . The error processes and initial conditions are assumed to be distributed normally, that is $\eta_{ij} \sim \mathcal{N}(0, \sigma_\eta^2)$, $u_{ij} \sim \mathcal{N}(0, \sigma_u^2)$, and $\epsilon_{i0} \sim \mathcal{N}(0, \sigma_{\epsilon_0}^2)$.

The moments we use to identify the parameters are the variances and first-order autocovariances. These moments can be written in closed form as follows:

$$\begin{aligned}\text{var}(\omega_{ij}) &= \rho^{2j}\sigma_{\epsilon_0}^2 + \frac{1 - \rho^{2j}}{1 - \rho^2}\sigma_u^2 + \sigma_\eta^2 \\ \text{cov}(\omega_{ij}, \omega_{ij-k}) &= \rho^k \frac{1 - \rho^{2(j-k)}}{1 - \rho^2}\sigma_u^2 + \rho^{2j-k}\sigma_{\epsilon_0}^2.\end{aligned}$$

These expressions are functions of (j, k) and the four parameters.

The estimation of the wage process uses the minimum distance estimator introduced by Chamberlain (1984), which minimizes a weighted squared sum of the differences between each moment in the model and its data counterpart. Let $m(\Lambda)$ be the vector of theoretical covariances and Λ be the parameter vector. The data counterpart is given by \hat{m} . In this case, the estimator solves:

$$\min_{\Lambda} (\hat{m} - m(\Lambda))' W (\hat{m} - m(\Lambda)),$$

where W is a weighting matrix. For our baseline parameterization, we use the identity matrix for W . To compute confidence intervals, we bootstrap using 1,000 replications. Given the closed form expressions for the theoretical moments, the objective function is efficiently evaluated.

We use the estimated parameters ρ and σ_u^2 to parameterize the residual wage process in the model.⁴ The results of our estimation procedure are reported in Table 5. We find the parameters are precisely estimated with estimates for $\hat{\rho}$ in the range of 0.95 to 0.97 across education groups. If we construct estimates of variation for the residual wages, that is, $\hat{\sigma}_u^2/(1 - \hat{\rho}^2)$, we find that households with a low and high member and those with two high members are close to twice as variable as the others.

⁴ We assume η is a shock that households can insure against, and we use the ergodic distribution based on ρ and σ_u^2 to parameterize the initial distribution of productivities.

In Figure 4, we report the life-cycle wage profiles (ζ_j) for the 6 education groups. The right side of the figure shows the population for each group. For example, the low-low group is the largest with 43 percent of the working population. We have normalized these estimates by dividing each profile using the average wage rate for the entire population. Not surprising, we find a steep rise between ages 25 and 45 for all groups, with the lowest higher by roughly 40 percent and the highest by roughly 200 percent.

3.3. Computation

When we compute equilibria for our positive economy and our reform problem, we approximate labor productivity shocks by a Markov chain with 20 types. For both problems we assume that baseline preferences are logarithmic, that is,

$$U(c, \ell) = \gamma \log c + (1 - \gamma) \log \ell. \quad (3.1)$$

Both problems are parallelizable and thus we can solve them quickly on most modern computer clusters. As a check on these choices, we will recompute results for a 40-type case and for different preferences.

4. Results

In this section, we report our main findings for the baseline model and several alternative parameterizations, namely, cases with double the number of types, alternative preferences, no wage growth, and lower variances in the shock processes.

4.1. Baseline

The main deliverables for our baseline model are labor wedges and welfare gains. We compute labor wedges for each education group. These wedges represent distortions used

by the planner to incentivize individuals and to provide insurance across time and across types. We then report consumption-equivalent welfare gains and their decomposition into gains from increasing the level of consumption, gains from reducing dispersion in consumption, gains from increasing the level of leisure, and gains from reducing the dispersion in leisure.

The labor wedges are defined as follows:

$$\tau_n(\epsilon^j) = 1 - \frac{1}{w} \frac{U_\ell(c(\epsilon^j), \ell(\epsilon^j))}{U_c(c(\epsilon^j), \ell(\epsilon^j))} \quad (4.1)$$

and computed for each education group. Equation (4.1) tells us that in the optimal allocation there is a wedge between the wage rate w and the marginal rate of substitution between consumption and leisure. We report these wedges for the baseline model in Figure 5. The highest wedge is not that of the high-high group, but rather the low-high group. The reason is that the low-high group has the most variable wage process. The greater the dispersion in productivities, the greater are gains from insurance and higher is $\tau_n(\epsilon^j)$. In fact, if we were to take averages, we would find a positive correlation between the total variance $\hat{\sigma}_u^2/(1 - \hat{\rho}^2)$ and the wedge across education groups. This information is useful for the reform of current policy.

In Table 6, we report the welfare gains and its decomposition for our baseline parameterization. We find a total gain of 17 percent for an efficient reform in which all individuals are made better off by the same percentage. Building on Floden (2001) and Benabou (2002), we decompose this total gain into the gain from increasing consumption, the gain from smoothing consumption, the gain from increasing leisure, and the gain from smoothing leisure. That is, we take the total consumption-equivalent gain Δ and compute:

$$\log(1 - \Delta) = \log((1 - \Delta_c^L)(1 - \Delta_c^D))$$

$$+ (1 - \gamma) \log ((1 - \Delta_\ell^L) (1 - \Delta_\ell^D)) / \gamma.$$

Let x be the allocation in the planner problem and \hat{x} be the allocation in the positive economy. Then we define the gain due to a level increase in $x = \{c, \ell\}$ as

$$1 - \Delta_x^L = \frac{\sum \pi(\epsilon^j) \hat{x}(\epsilon^j)}{\sum \pi(\epsilon^j) x(\epsilon^j)}.$$

We define the gain due to a reduction in dispersion in $x = \{c, \ell\}$ as:

$$\begin{aligned} 1 - \Delta_x^D &= \sum \beta^j \pi(\epsilon^j) \log \left(\frac{\hat{x}(\epsilon^j)}{\sum \pi(\epsilon^j) \hat{x}(\epsilon^j)} \right) \\ &\quad - \sum \beta^j \pi(\epsilon^j) \log \left(\frac{x(\epsilon^j)}{\sum \pi(\epsilon^j) x(\epsilon^j)} \right) \end{aligned}$$

The results of the decomposition are shown in Table 6. First, note that the summing across rows yields the total gain of 17 percent (and may be off because of rounding). Second, note that there are large gains for increasing and smoothing consumption, but the optimal plan calls for lower and more dispersed leisure than in the positive economy. The gains from increasing consumption are the most significant. For the low-high and high-high groups, there are also significant gains from reducing dispersion since the variances of wages are largest for these groups. The planner lowers leisure the most for the most productive. However, in terms of leisure dispersion, the most noteworthy group is high-high that face significantly more leisure dispersion under the optimal plan relative to the positive economy.

If we consider these results in light of more simple models—say, static models with and without insurance—we find that our results are in line with the simpler models. For example, consider the case in which there is no insurance and households maximize (3.1) subject to a budget constraint that consumption is less than or equal to after-tax labor

earnings. The optimal plan in that case calls for variation in consumption but constant leisure. If instead there was full insurance, a planning problem would call for constant consumption and variation in leisure. The positive economy is closer to the no-insurance case and the reform problem is closer to the full-insurance case.

In Figure 6, we show the allocations of (log) consumption and leisure along with their variances for those in the low-low group. In the upper left panel of the figure, we have plotted consumption for ages 25 to 64. We see from the figure that the planner can completely smooth mean consumption, which is not possible under current policy due to the borrowing constraint. In the upper right panel of the figure, we have plotted the variance of consumption. Dispersion is lowered in early years, but is higher than the positive economy later in life. In the lower panels, we plot the results for leisure. As predicted, leisure is lower in the reform problem than the positive economy for most years, while the variance is higher.

4.2. Sensitivity

We recompute total consumption-equivalent gains and their decomposition in three alternate specifications. First, we double the number of types from 20 to 40. Second, we consider alternative preferences with a lower Frisch elasticity. Third, we set the wage profiles in Figure 4 to 1 for all types and all ages. Fourth, we lower the variance σ_u^2 of the labor productivity shocks for all education groups. In each case, we compare results for the levels and dispersion of allocations across ages for the low-low group to the baseline model.

The first set of results are shown in Table 7. In this case, we find a slightly lower overall welfare gain of 16 percent in the case with 40 types (and again 16 percent if we

continue increasing the number of types). If we compare the decomposition of gains with the baseline model, we find only small differences. Similarly, if we compute statistics over the life cycle, we find that the differences are not large. This is evident in Figure 7 where we compare the allocations—both levels and variances—for the two models. We see almost no change in levels and small changes in the variances of the allocations.

In Table 8, we report results for an alternative specification of preferences, namely,

$$U(c, \ell) = \gamma \log c - \kappa \frac{(1 - \ell)^\alpha}{\alpha} \quad (4.2)$$

which has a constant Frisch elasticity that we set equal to 1/2 (by setting $\alpha = 3$). In this case, the overall welfare gain is 14 percent and the decomposition, not surprisingly, shows a smaller contribution from lowering dispersion in leisure. Figure 8 shows the comparison of the baseline statistics with those for these alternative preferences for the low-low group. Consistent with the welfare decomposition, we find little difference between means and variances of leisure in the positive and reform economies. In the case of consumption, there are some differences in the levels of means and variances, but the shifts are similar in the case of both economies.

If we set wage profiles equal to 1 for all ages and groups, we find a lower overall gain of 14 percent when compared to the 17 percent gain in the baseline. In Table 9, we see that the main difference between these models is the attribution of gains for smoothing consumption. If the profiles are flat, there are no gains to smoothing consumption: they are already smooth. In the case of the low-low group, we see in Figure 9 that the positive economy consumption and leisure allocations are already quite flat.

Finally, we compare the baseline model to one with the labor productivity variance σ_u^2 lowered by two-thirds. The overall gain in the latter case is 19 percent, higher than the

baseline and, not surprising, the gains for reducing consumption and leisure dispersion are less significant than gains from changing levels. These results are reported in Table 10. In Figure 10, we again compare allocations to the baseline model for the low-low group. Here, we find no difference in the levels, but lower variances for consumption and leisure in the alternative model when compared to the baseline.

In all experiments, we find large gains to the Pareto reforms, but the sources of the gains do depend on the estimated processes for labor productivities.

5. Conclusion

In this paper, we computed efficiency gains of Pareto reforms in an environment with policies constrained due to private information about shocks to household labor productivity. Using administrative data for the Netherlands, we found the gains to be large but also found that quantifying the sources of these gains depends importantly on having precise estimates for household wage profiles and shock processes for labor productivity.

Appendix

In the main text we present a planning problem and discuss how we characterize its solution using relaxed and recursive household planning problems. In this appendix we describe the intermediate steps. We start with a general specification of the planning problem to be solved and our notion of efficiency. We then describe steps to be taken to compute a solution. Our discussion closely follows Boerma (2019).

The problem for the planner is to maximize the present value of aggregate resources subject to incentive constraints and meeting minimum bounds on lifetime utility for all households. A household i is identified by a birth year b and a history of shocks to productivities ϵ^{j-1} at the time of the reform, that is, $i \equiv (b, \epsilon^{j-1})$. The set of households considered by the planner at the time of the reform includes those currently alive and those that will be born in future periods. In period 1, this set is:

$$\mathcal{I} \equiv \left\{ \left\{ (1-j, \epsilon^{j-1}) \right\}_{j=1}^J, \left\{ (b, \epsilon_0) \right\}_{t=1}^{\infty} \right\}.$$

We use the notation $x(i)$ for household $i = (t, \epsilon^{j-1})$'s allocation of consumption and labor:

$$x(i) \equiv \left\{ x_{b+s}(\epsilon^s) \right\}_{s=1}^J,$$

where $x_{b+s}(\epsilon^s) = (c_{b+s}(\epsilon^s), n_{b+s}(\epsilon^s))$. We use the notation x to summarize both the allocations of all households and the aggregate quantities of consumption C_t , hours N_t , end-of-period holdings of foreign assets B_{t+1} , and end-of-period capital K_{t+1} :

$$x \equiv \left\{ \left\{ x(i) \right\}_{\mathcal{I}}, \left\{ (C_t, N_t, B_{t+1}, K_{t+1}) \right\}_{t=1}^{\infty} \right\}.$$

We study a small open economy and assume the returns on assets are given by rate R and that capital depreciates at rate δ , with the aggregate resource constraint given by:

$$C_t + K_{t+1} - (1 - \delta) K_t + G_t + B_{t+1} \leq F(K_t, N_t) + RB_t.$$

The aggregate consumption and hours can be written as:

$$C_t = \sum_{j=1}^J \int_{\mathcal{E}^j} c_t(\epsilon^j) d\mu_j(\epsilon^j)$$

$$N_t = \sum_{j=1}^J \int_{\mathcal{E}^j} \epsilon_j \zeta_j n_t(\epsilon^j) d\mu_j(\epsilon^j),$$

where ζ_j is the deterministic age profile of productivity.

Households have private information about the history of productivity shocks, so we need to specify the information sets and the reporting strategies of households. Here, we assume that households make a report $m_j \in \mathcal{E}_j$ at age j about their type ϵ_j , where \mathcal{E}_j is the set of all possible productivities at age j . A strategy specifies a report for every productivity history, $\sigma = \{\sigma_j(\epsilon^j)\}_{\epsilon^j, j}$, where σ_j maps the history of shocks to the current message, that is, $\sigma_j : \epsilon^j \rightarrow m_j$. The history of reports is summarized as:

$$\sigma^j(\epsilon^j) = (\sigma_1(\epsilon^1), \dots, \sigma_j(\epsilon^j)).$$

The maximization problem for the planner is:

$$\max_x \sum_{t=1}^T R^{-t} (wN_t - C_t) + K_0 + B_0 - \sum_{t=1}^T G_t/R^t$$

subject to the following constraints for all i, j_i , and all reporting strategies σ :

$$\sum_{j=j_i}^J \beta^{j-j_i} \int_{\mathcal{E}^j} U(c_t(\epsilon^j), n_t(\epsilon^j)) \geq \sum_{j=j_i}^J \beta^{j-j_i} \int_{\mathcal{E}^j} U(c_t(\sigma^j(\epsilon^j)), n_t(\sigma^j(\epsilon^j))) \quad (5.1)$$

$$\sum_{j=j_i}^J \beta^{j-j_i} \int_{\mathcal{E}^j} U(c_{b+j}(\epsilon^j), n_{b+j}(\epsilon^j)) d\mu_j(\epsilon^j | \epsilon^{j_i}) \geq v_0(i), \quad (5.2)$$

where the marginal product of labor w and promised values $v_0(i)$, all i , are given, and j_i is the age for currently-alive households i at the time of the reform and j_i is 1 for all future households.

We are interested in allocations that are efficient in the sense that there is no alternative incentive and resource feasible allocation that makes all households weakly better off and some strictly better off.

Proposition. Let $v_0(i)$ be:

$$v_0(i) = \sum_{j_i}^J \beta^{j-1} \int_{\mathcal{E}^j} U(c_{b+j}(\epsilon^j), n_{b+j}(\epsilon^j)) d\mu(\epsilon^j | \epsilon^{j_i}), \quad (5.3)$$

where the c and n are consumption and hours in allocation x . Then, allocation x is efficient if and only if it solves the planner problem with a maximum of zero, given the promised values in (5.3).

Proof. We show both directions by contradiction. \Rightarrow If an allocation x is efficient it solves the planner problem given $v_0(i)$ for all $i \in \mathcal{I}$ with a maximum of zero. Suppose x does not solve the planner problem and let \hat{x} denote a solution to the planner problem. Because x is feasible, the allocation \hat{x} generates strictly excess resources in the first period. Construct an alternative allocation \tilde{x} identical to \hat{x} but increase initial consumption such that the incentive constraints in (5.1) are satisfied. The allocation \tilde{x} strictly Pareto dominates x , which is a contradiction.

\Leftarrow If an allocation x solves the planner problem given $v_0(i)$ for all $i \in \mathcal{I}$ with a zero maximum, then it is efficient. Suppose that x is not efficient, then there exists an alternative feasible allocation \hat{x} such that all households are better off, with some household i strictly better off. Since \hat{x} is feasible and delivers at least $v_0(i)$ for all $i \in \mathcal{I}$, \hat{x} is a candidate solution to the planner problem. Construct an alternative allocation \tilde{x} , which is equal to \hat{x} but reduce initial consumption for household i that is strictly better off under \hat{x} (such that the incentive constraints are satisfied). Alternative allocation \tilde{x} is feasible and generates

excess resources in the initial period. This contradicts that x is a solution to the planner problem. ■

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FIGURE 1. PARETO EFFICIENT FRONTIER

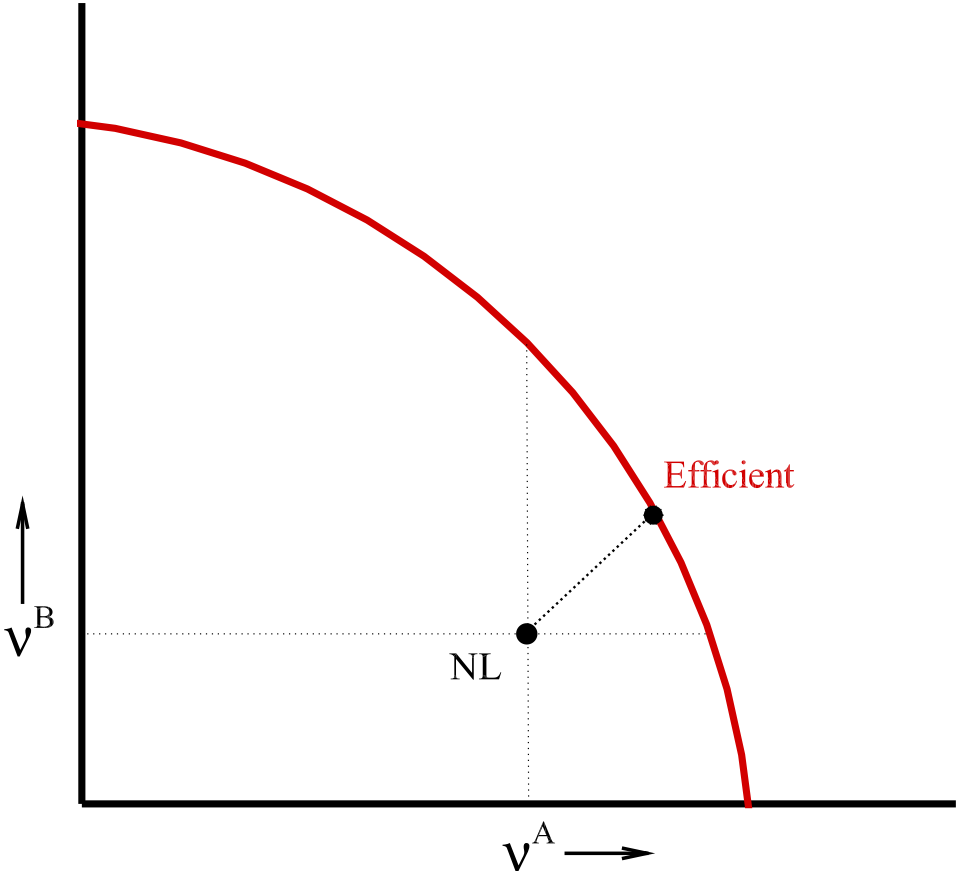


FIGURE 2. INCOME TAX SCHEDULE

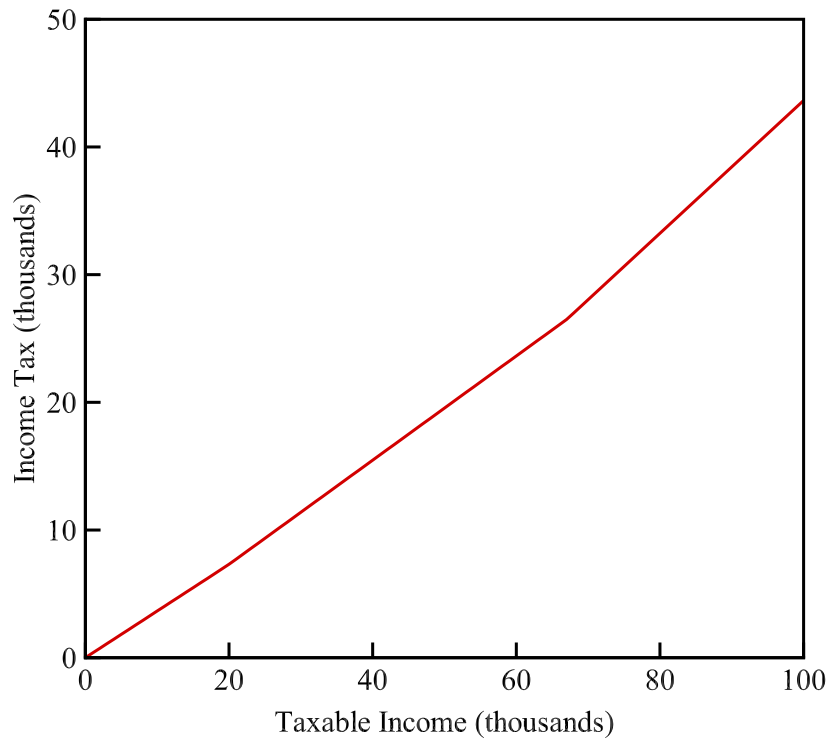


FIGURE 3. FINANCIAL ASSET TAX SCHEDULE

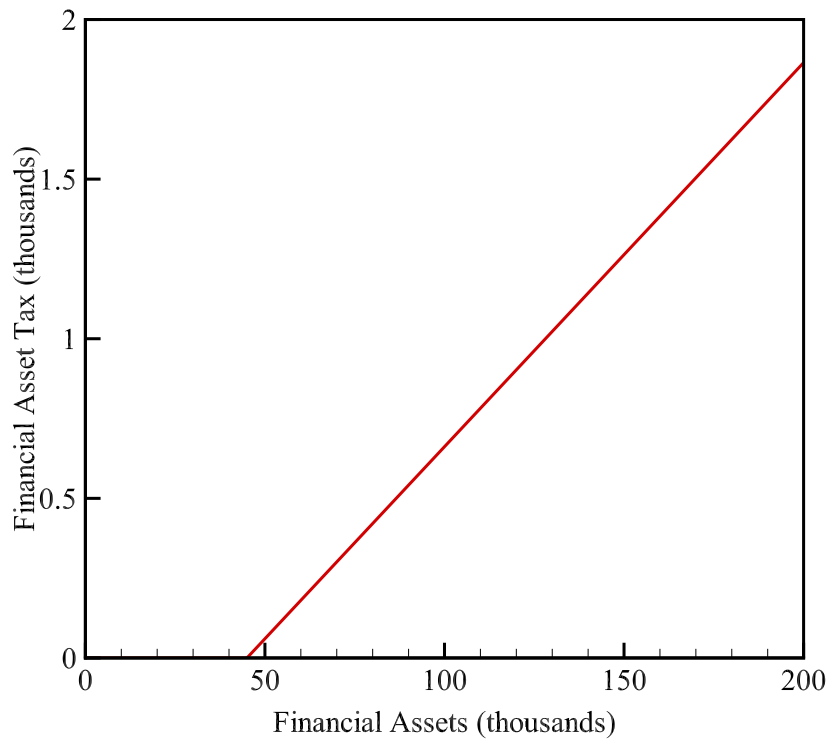


FIGURE 4. WAGE PROFILES

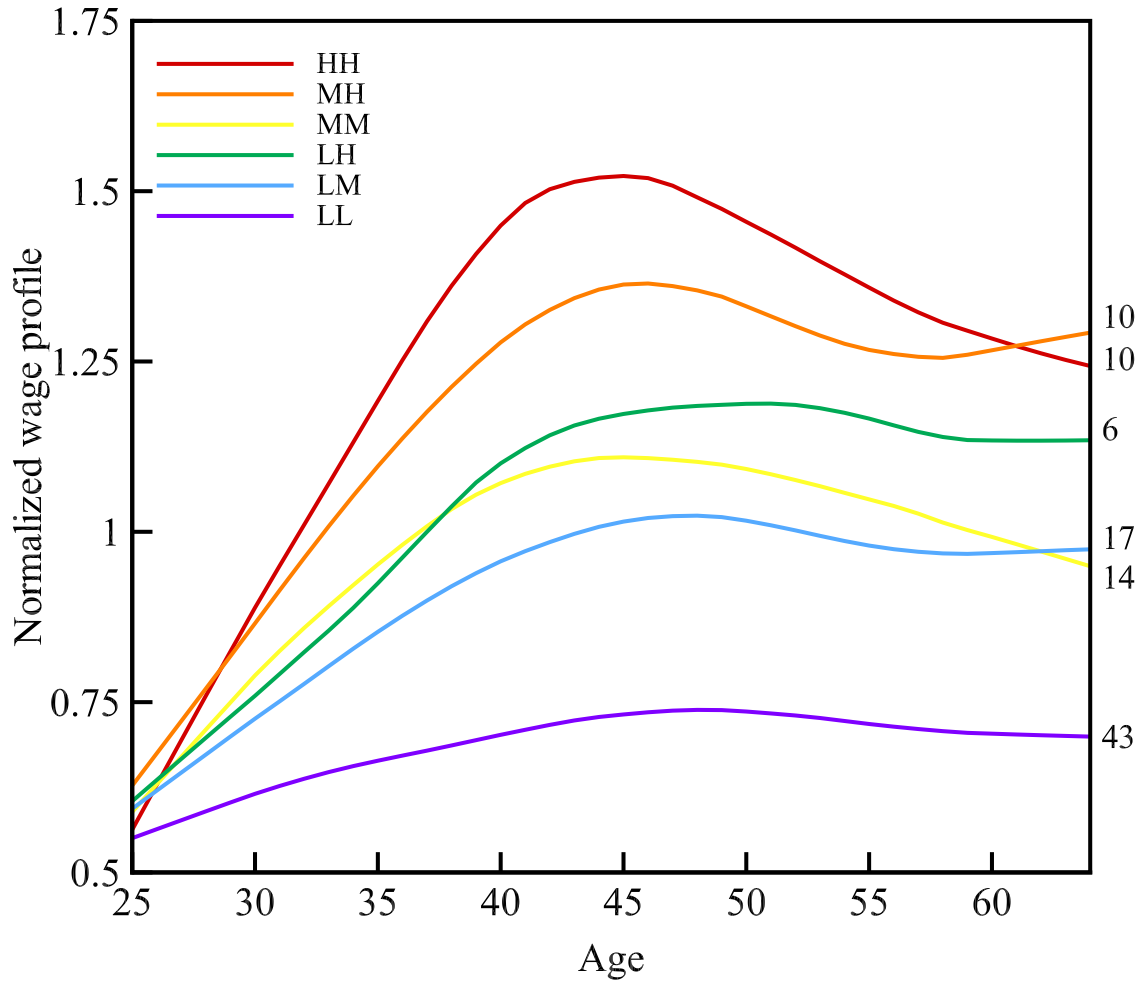


FIGURE 5. LABOR WEDGES: BASELINE MODEL

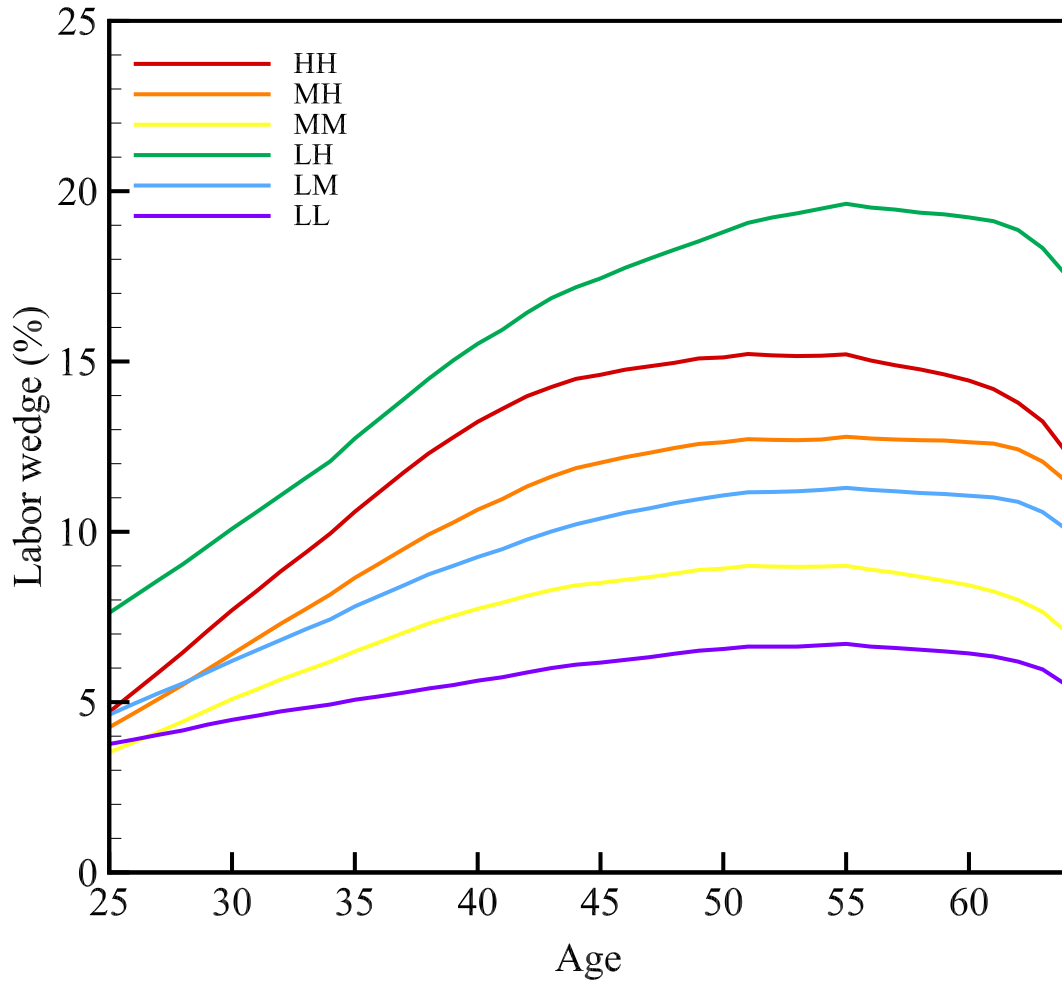
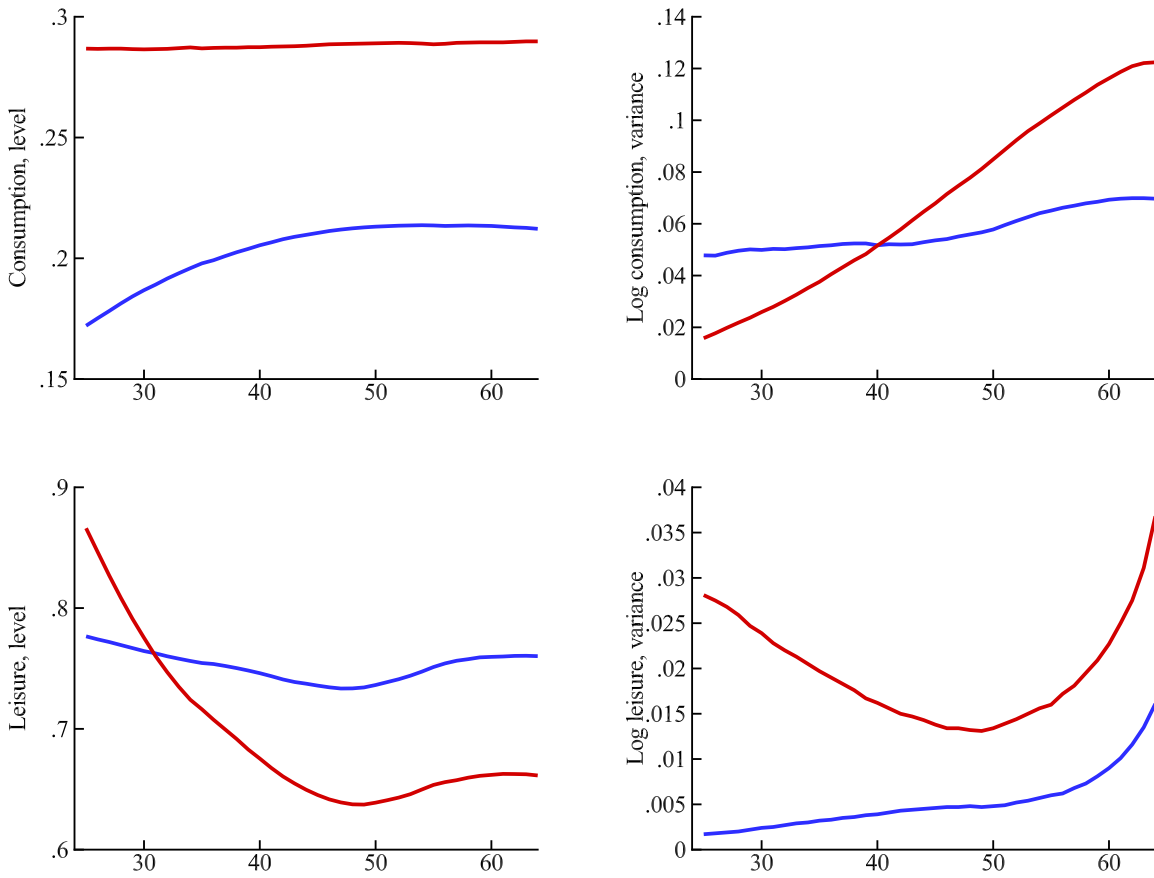
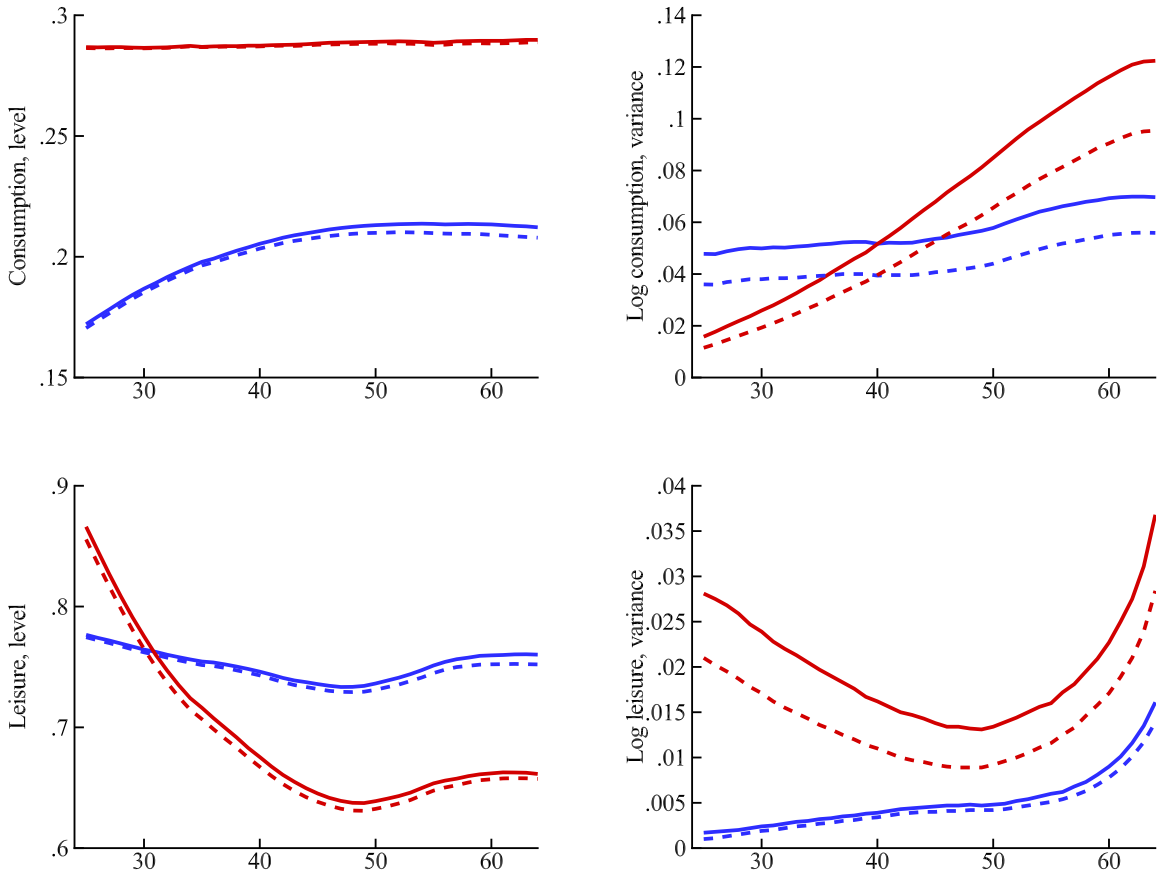


FIGURE 6. ALLOCATION LEVELS AND DISPERSION FOR LL: BASELINE MODEL



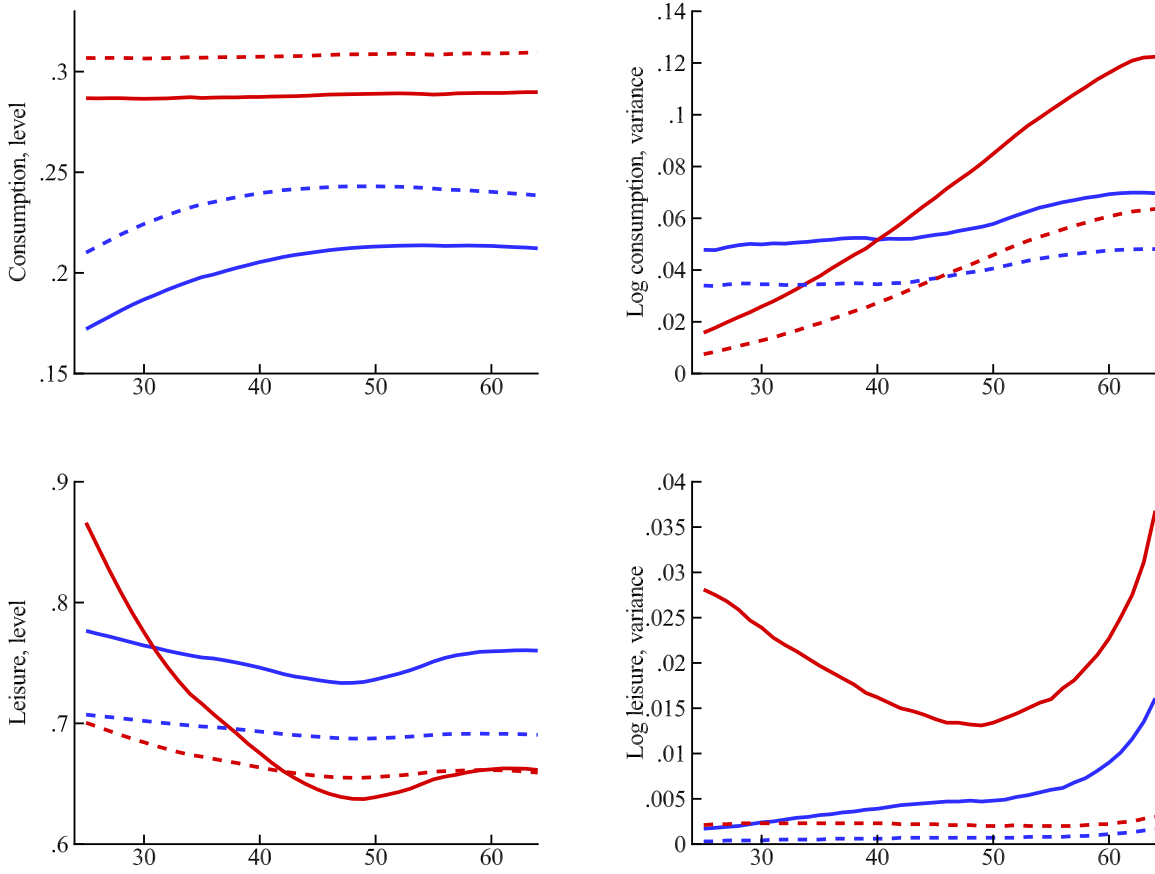
Note: Results for the positive economy are shown in blue and results for the reform problem are shown in red.

FIGURE 7. ALLOCATION LEVELS AND DISPERSION FOR GROUP LOW-LOW
 Comparison of Baseline and 40-Types Model



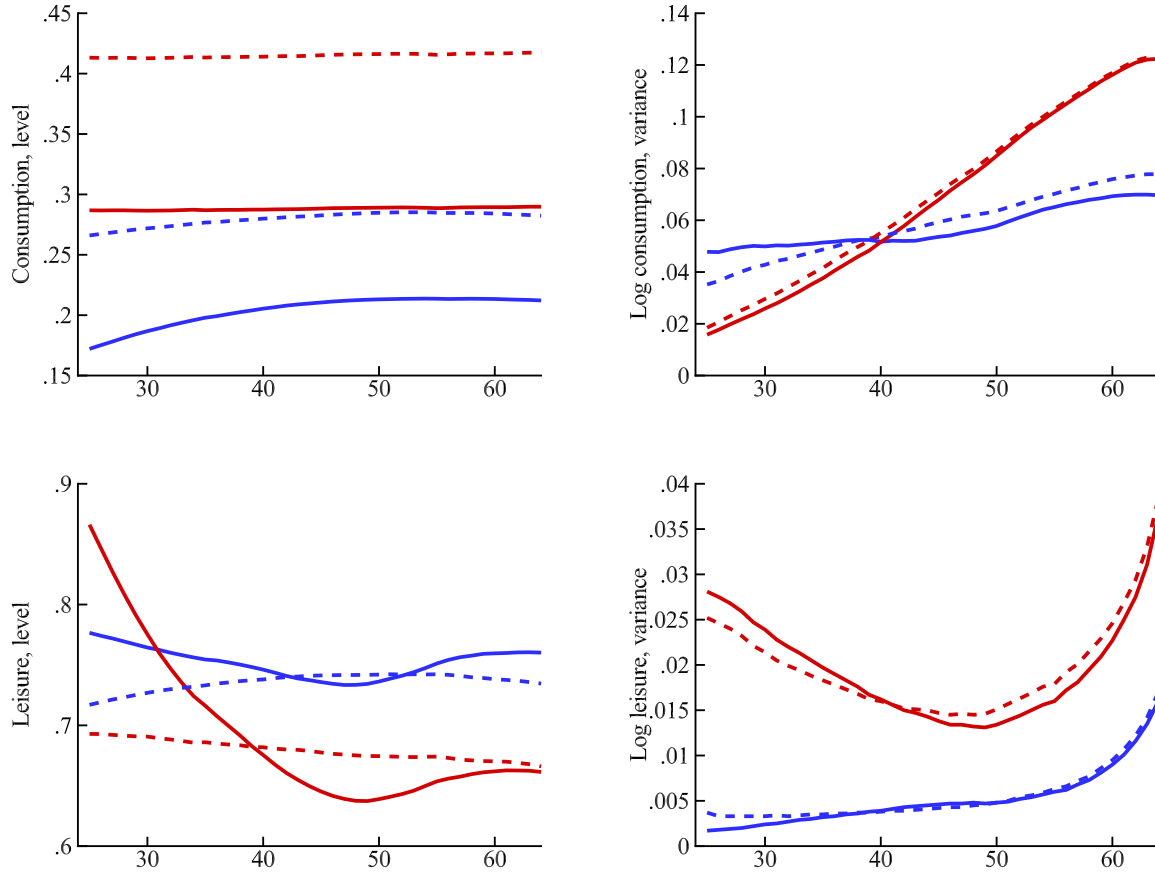
Note: Results for the positive economy are shown in blue and results for the reform problem are shown in red. The solid lines are the baseline model and the dashed lines are the 40-type model.

FIGURE 8. ALLOCATION LEVELS AND DISPERSION FOR GROUP LOW-LOW
 Comparison of Baseline and Alternative Preferences



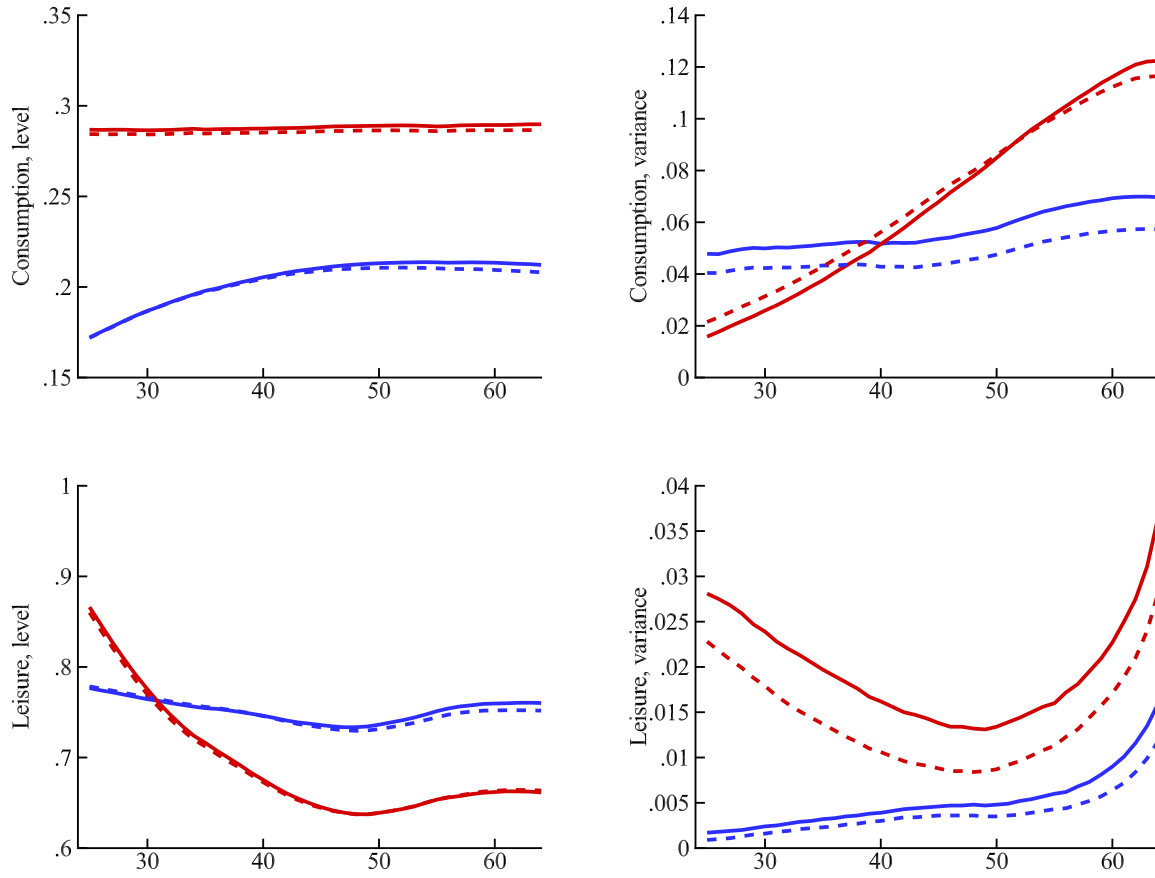
Note: Results for the positive economy are shown in blue and results for the reform problem are shown in red. The solid lines are the baseline model and the dashed lines are the model with constant Frisch elasticity preferences.

FIGURE 9. ALLOCATION LEVELS AND DISPERSION FOR GROUP LOW-LOW
 Comparison of Baseline and No Wage Growth Model



Note: Results for the positive economy are shown in blue and results for the reform problem are shown in red. The solid lines are the baseline model and the dashed lines are the no-wage-growth model.

FIGURE 10. ALLOCATION LEVELS AND DISPERSION FOR GROUP LOW-LOW
 Comparison of Baseline and Lower Shock Variance Model



Note: Results for the positive economy are shown in blue and results for the reform problem are shown in red. The solid lines are the baseline model and the dashed lines are the lower-shock-variance model.

TABLE 1. REVISED NATIONAL INCOME AND PRODUCT ACCOUNTS
 AVERAGES RELATIVE TO ADJUSTED GDP, 2000–2010

TOTAL ADJUSTED INCOME	1.000
Labor Income	.566
Compensation of employees	.502
Wages and salary accruals	.397
Supplements to wages and salaries	.105
70% of proprietors' income	.064
Capital Income	.434
Profits	.156
30% of proprietors' income	.027
Indirect business taxes	.105
<i>Less:</i> Sales tax	.103
Consumption of fixed capital	.165
Consumer durable depreciation	.050
Imputed capital services	.035
Consumer durable services	.012
Government capital services	.023

See footnotes at the end of the table.

TABLE 1. REVISED NATIONAL INCOME AND PRODUCT ACCOUNTS
 AVERAGES RELATIVE TO ADJUSTED GDP, 2000–2010 (CONT.)

TOTAL ADJUSTED PRODUCT	1.000
Consumption	.635
Personal consumption expenditures	.484
<i>Less:</i> Consumer durable goods	.068
<i>Less:</i> Imputed sales tax, nondurables and services	.088
<i>Plus:</i> Imputed capital services, durables	.012
Government consumption expenditures, nondefense	.222
<i>Plus:</i> Imputed capital services, government capital	.023
Consumer durable depreciation	.050
Tangible investment	.351
Gross private domestic investment	.177
Consumer durable goods	.068
<i>Less:</i> Imputed sales tax, durables	.014
Government gross investment, nondefense	.041
Net exports of goods and services	.079
Defense spending	.014

Note: The data source for national income statistics is the Dutch Bureau of Statistics. Imputed capital services are equal to 4 percent times the current-cost net stock of government fixed assets and consumer durable goods.

TABLE 2. REVISED FIXED ASSET TABLES WITH STOCKS END OF PERIOD,
AVERAGES RELATIVE TO ADJUSTED GDP, 2000–2010

TOTAL CAPITAL	5.657
Fixed assets	3.068
Businesses	1.261
Government	0.571
Households	1.236
Consumer durables	.301
Inventories	.142
Businesses	.129
Households	.013
Land	1.905
Agricultural and productive land	.420
Residential land	1.485
Oil and gas	.241

Note: The data source for national income statistics is the Dutch Bureau of Statistics.

TABLE 3. HOUSEHOLD NET WORTH AND GOVERNMENT DEBT
AVERAGES RELATIVE TO ADJUSTED GDP, 2000–2010

HOUSEHOLD NET WORTH, END OF PERIOD	3.895
Assets	5.130
Tangible	2.466
Financial	2.664
Liabilities	1.236
GOVERNMENT DEBT, END OF PERIOD	.556

Note: The data source for national income statistics is the Dutch Bureau of Statistics.

TABLE 4. POPULATION, EMPLOYMENT, AND HOURS
AVERAGES, 2000–2010

POPULATION IN MILLIONS	
All ages	16.3
Ages 16 to 64	10.8
POPULATION GROWTH (%)	
All ages	0.5
Ages 16 to 64	0.3
ANNUAL HOURS PER POPULATION 16-64	1,135

Note: The data source for national income statistics is the Dutch Bureau of Statistics.

TABLE 5. ESTIMATED WAGE PROCESS PARAMETERS

Education Group	Persistence		Innovation Variance	
	$\hat{\rho}$	Confidence	$\hat{\sigma}_u^2$	Confidence
Low, Low	.9542	(.9515,.9575)	.0096	(.0093,.0102)
Low, Medium	.9660	(.9610,.9692)	.0087	(.0083,.0096)
Low, High	.9673	(.9628,.9710)	.0162	(.0153,.0176)
Medium, Medium	.9570	(.9536,.9612)	.0099	(.0091,.0103)
Medium, High	.9616	(.9520,.9782)	.0109	(.0082,.0124)
High, High	.9564	(.9501,.9582)	.0172	(.0164,.0184)

TABLE 6. WELFARE GAIN DECOMPOSITION: BASELINE MODEL
TOTAL WELFARE GAIN OF 17%

Education group	Consumption		Leisure	
	Δ_c^L	Δ_c^D	Δ_ℓ^L	Δ_ℓ^D
Low, Low	22	2	-11	4
Low, Medium	21	3	-12	5
Low, High	16	5	-10	6
Medium, Medium	21	3	-13	5
Medium, High	19	5	-14	6
High, High	17	8	-15	7

TABLE 7. WELFARE GAIN DECOMPOSITION: 40 TYPES MODEL
TOTAL WELFARE GAIN OF 16%

Education group	Consumption		Leisure	
	Δ_c^L	Δ_c^D	Δ_ℓ^L	Δ_ℓ^D
Low, Low	22	1	-11	4
Low, Medium	21	3	-12	6
Low, High	17	5	-13	7
Medium, Medium	21	3	-13	5
Medium, High	20	5	-15	7
High, High	17	6	-15	7

TABLE 8. WELFARE GAIN DECOMPOSITION: ALTERNATIVE PREFERENCES
TOTAL WELFARE GAIN OF 14%

Education group	Consumption		Leisure	
	Δ_c^L	Δ_c^D	Δ_ℓ^L	Δ_ℓ^D
Low, Low	17	1	-4	1
Low, Medium	15	2	-4	1
Low, High	13	4	-4	0
Medium, Medium	16	2	-5	1
Medium, High	15	3	-5	1
High, High	13	6	-6	1

TABLE 9. WELFARE GAIN DECOMPOSITION: NO GROWTH MODEL
TOTAL WELFARE GAIN OF 14%

Education group	Consumption		Leisure	
	Δ_c^L	Δ_c^D	Δ_ℓ^L	Δ_ℓ^D
Low, Low	28	0	-9	1
Low, Medium	27	0	-7	1
Low, High	25	0	-5	1
Medium, Medium	28	0	-8	1
Medium, High	27	0	-7	1
High, High	25	1	-6	1

TABLE 10. WELFARE GAIN DECOMPOSITION: LOWER VARIANCE MODEL
TOTAL WELFARE GAIN OF 19%

Education group	Consumption		Leisure	
	Δ_c^L	Δ_c^D	Δ_ℓ^L	Δ_ℓ^D
Low, Low	26	1	-12	4
Low, Medium	27	3	-19	7
Low, High	25	6	-21	8
Medium, Medium	26	3	-17	7
Medium, High	26	6	-21	8
High, High	21	7	-17	8